

Factoring Trinomials

Trinomials usually come about when we multiply two binomials:

$$(x + 3)(x + 5)$$

using **FOILING** we can evaluate the above as follows: $x^2 + 5x + 3x + 15$ and we simplify to $x^2 + 8x + 15$

But what if we started with $x^2 + 8x + 15$ and were asked factor it (bring it back to its beginnings)?

How could we return $x^2 + 8x + 15$ back to its original state of $(x + 3)(x + 5)$? This process is known as **FACTORING**

Before we start let us look at the various forms a trinomial can be found in

A TRINOMIAL is in this basic form $ax^2 + bx + c$ examples:

- $x^2 + 8x + 15$
- $x^2 + 5x + 6$
- $x^2 + x - 6$
- $3x^2 + 15x + 18$
- $6x^2 + 13x - 5$

For each one of the above examples identify what a, b, and c are for each trinomial

We will use the same basic way to factor **BUT** how we proceed and finish will depend on whether $a = 1$ or whether $a \neq 1$

Factoring $ax^2 + bx + c$ where $a = 1$

Method: Product / Sum (x and +)

Example: $x^2 + 8x + 15$

STEP 1: Determine what "a", "b", and "c" are.

$a = 1$, $b = 8$, and $c = 15$

STEP 2: Create a product/sum table

| | |
|---|---|
| x | + |
| | |

STEP 3: To determine what product / sum you are looking for you will do the following:

to get your product # multiply " $a \times c$ " and to find your sum # simply write in the value of "b"

therefore your product is $1 \times 15 = 15$ and your sum is 8

| | |
|----|---|
| 15 | 8 |
| x | + |
| | |

STEP 4: Determine two numbers that multiply to give you your product number and add up to give you your sum number

| | |
|-------|---|
| 15 | 8 |
| x | + |
| 5 , 3 | |

STEP 5: Take these two numbers and place them in brackets with an x at each start

$(x + 5)(x + 3)$ is your answer

Step 6: Check. How? take answer $(x + 5)(x + 3)$ and **FOIL and SIMPLIFY**.

$$\begin{aligned}(x + 5)(x + 3) &= x^2 + 5x + 3x + 15 \\ &= x^2 + 8x + 15\end{aligned}$$

Factoring $ax^2 + bx + c$ where $a \neq 1$

Method: Product / Sum (x and $+$)

Example: $3x^2 + 15x + 18$

FIRST THOUGHT when $a \neq 1$, can “a” be factored out from all terms, if YES factor “a” out from all terms and proceed with product / sum just like you did when $a = 1$

STEP 1: $a \neq 1$ $3x^2 + 15x + 18$, factor 3 out because $a = 3$ from all terms $3(x^2 + 5x + 6)$

STEP 2: Determine what “a”, “b”, and “c” are.

$a = 1$, $b = 5$, and $c = 6$

STEP 3: Create a product/sum table

| | |
|---|---|
| x | + |
| | |

STEP 4: To determine what product / sum you are looking for you will do the following:

to get your product # multiply “a x c” and to find your sum # simply write in the value of “b”

therefore your product is $1 \times 6 = 6$ and your sum is 5

| | |
|---|---|
| 6 | 5 |
| x | + |
| | |

STEP 5: Determine two numbers that multiply to give you your product number and add up to give you your sum number

| | |
|------|---|
| 6 | 5 |
| x | + |
| 3, 2 | |

STEP 6: Take these two numbers and place them in brackets with an x at each start. **MAKE CERTAIN TO INCLUDE THE NUMBER YOU FACTORED OUT IN YOUR FINAL ANSWER.**

$3(x + 3)(x + 2)$ is your answer

Step 7: Check. How? take answer $3(x + 3)(x + 2)$ and **FOIL and SIMPLIFY.**

$$\begin{aligned} 3(x + 3)(x + 2) &= (3x + 9)(x + 2) \\ &= 3x^2 + 6x + 9x + 18 \\ &= 3x^2 + 15x + 18 \end{aligned}$$

Factoring $ax^2 + bx + c$ where $a \neq 1$

Method: Product / Sum (x and +)

Example: $6x^2 + 13x - 5$

FIRST THOUGHT when $a \neq 1$, can it be factored out from all terms, if NO you still proceed with product / sum

STEP 1: Determine what "a", "b", and "c" are.

$$a = 6, b = 13, \text{ and } c = -5$$

STEP 2: Create a product/sum table

| x | + |
|---|---|
| | |

STEP 3: To determine what product / sum you are looking for you will do the following:

to get your product # multiply "a x c" and to find your sum # simply write in the value of "b"

therefore your product is $6 \times (-5) = -30$ and your sum is **13**

| -30 | 13 |
|-----|----|
| x | + |
| | |

STEP 4: Determine two numbers that multiply to give you your product number and add up to give you your sum number

| -30 | 13 |
|--------|----|
| x | + |
| 15, -2 | |

STEP 5: **Because "a" does not equal 1, we cannot simply place the two numbers in the brackets and we are done.** We need to do the following: Take these two numbers and place them in brackets BUT where you would normally place an x you would now have to place an x and whatever the "a" value is.

$$(6x + 15) (6x - 2)$$

STEP 6: **SIMPLIFY EACH BRACKET BY REDUCING EACH TO LOWEST TERMS**

$(6x + 15)$ can be reduced by 3 and $(6x - 2)$ can be reduced by 2

Result $(6x + 15) (6x - 2)$ becomes **$(2x + 5) (3x - 1)$**

STEP 7: **Check. How? take answer $(3x - 1) (2x + 5)$ and FOIL and SIMPLIFY.**

$$\begin{aligned} (3x - 1) (2x + 5) &= 6x^2 + 15x - 2x - 5 \\ &= 6x^2 + 13x - 5 \end{aligned}$$